Archimedes Principle Worksheet Answers

More than 2,000 years ago, Archimedes discovered the relationship between buoyant force and how much fluid is displaced by an object. **Archimedes principle** states:

**The buoyant force acting on an object in a fluid is equal to the weight of the fluid displaced by the object.**

We can practice figuring out the buoyant force using a beach ball and a big tub of water. Our beach ball has a volume of 14,130 cm\(^3\). The weight of the beach ball in air is 1.5 N.

If you put the beach ball into the water and don’t push down on it, you’ll see that the beach ball floats on top of the water by itself. Only a small part of the beach ball is underwater. Measuring the volume of the beach ball that is under water, we find it is 153 cm\(^3\). Knowing that 1 cm\(^3\) of water has a mass of 1 g, you can calculate the weight of the water displaced by the beach ball.

153 cm\(^3\) of water = 153 grams = 0.153 kg

weight = mass × force of gravity per kg = (0.153 kg) × 9.8 N/kg = 1.5 N

According to Archimedes principle, the buoyant force acting on the beach ball equals the weight of the water displaced by the beach ball. Since the beach ball is floating in equilibrium, the weight of the ball pushing down must equal the buoyant force pushing up on the ball. We just showed this to be true for our beach ball.

Have you ever tried to hold a beach ball underwater? It takes a lot of effort! That is because as you submerge more of the beach ball, the more the buoyant force acting on the ball pushes it up. Let’s calculate the buoyant force on our beach ball if we push it all the way under the water.

Completely submerged, the beach ball displaces 14,130 cm\(^3\) of water. Archimedes principle tells us that the buoyant force on the ball is equal to the weight of that water:

14,130 cm\(^3\) of water = 14,130 grams = 14.13 kg

weight = mass × force of gravity per kg = (14.13 kg) × 9.8 N/kg = 138 N

If the buoyant force is pushing up with 138 N, and the weight of the ball is only 1.5 N, your pushing down on the ball supplies the rest of the force, 136.5 N.

A 10-cm\(^3\) block of lead weighs 1.1 N. The lead is placed in a tank of water. One cm\(^3\) of water weighs 0.0098 N. What is the buoyant force on the block of lead?

<table>
<thead>
<tr>
<th>Given:</th>
<th>Solution:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight of lead block = 1.1 N</td>
<td>The lead displaces 10 cm(^3) of water. buoyant force = weight of water displaced</td>
</tr>
<tr>
<td>Volume of block = 10 cm(^3)</td>
<td>10 cm(^3) of water × 0.0098 N/cm(^3) = 0.098 N</td>
</tr>
</tbody>
</table>

**Looking for:**
Buoyant force on the lead block

**Relationships:**
1 cm\(^3\) of water weighs 0.0098 N.
1. A block of gold and a block of wood both have the same volume. If they are both submerged in water, which has the higher buoyant force? Answer – if they are both submerged, they displace the same amount of fluid, therefore their buoyant force is the same.

2. A 100-cm$^3$ block of lead that weighs 11 N is carefully submerged in water. One cm$^3$ of water weighs 0.0098 N.
   a. What volume of water does the lead displace? Answer – 100 cm$^3$
   b. How much does that volume of water weigh? Answer – 0.0098 x 100 = 0.98 N
   c. What is the buoyant force on the lead? Answer - 0.98 N
   d. Will the lead block sink or float in the water? Answer - sink

3. The same 100-cm$^3$ lead block is carefully submerged in a container of mercury. One cm$^3$ of mercury weighs 0.13 N.
   a. What volume of mercury is displaced? Answer – 100 cm$^3$
   b. How much does that volume of mercury weigh? Answer – 0.13 x 100 = 13 N
   c. What is the buoyant force on the lead? Answer -13 N
   d. Will the lead block sink or float in the mercury? Answer - float

4. According to problems 2 and 3, does an object’s density have anything to do with whether or not it will float in a particular liquid? Justify your answer. Answer – if an object is denser than the fluid it is placed in it will sink, if the object is less dense than the fluid it will float.

5. Based on the table of densities, explain whether the object would float or sink in the following situations:

<table>
<thead>
<tr>
<th>material</th>
<th>density (g/ cm$^3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>gasoline</td>
<td>0.7</td>
</tr>
<tr>
<td>gold</td>
<td>19.3</td>
</tr>
<tr>
<td>lead</td>
<td>11.3</td>
</tr>
<tr>
<td>mercury</td>
<td>13.6</td>
</tr>
<tr>
<td>molasses</td>
<td>1.37</td>
</tr>
<tr>
<td>Paraffin(wax)</td>
<td>0.87</td>
</tr>
<tr>
<td>platinum</td>
<td>21.4</td>
</tr>
</tbody>
</table>

   a. A block of solid paraffin (wax) in molasses. Answer - floats
   b. A bar of gold in mercury. Answer - sink
   c. A piece of platinum in gasoline. Answer - sinks
   d. A block of paraffin in gasoline. Answer - sink